

$$\cos^4 x + \cos^4 x = 1 + \cos 2x - 2\sin^2 2x$$